

EXAM III Physics 208 2017

Last Name.....First Name .....Section Number.....

USEFUL INFORMATION

$$\vec{F} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2} \hat{r}$$

$$\vec{F} = q(\vec{v} \times \vec{B})$$

$$d\vec{B} = \frac{\mu_0 i}{4\pi} \frac{d\vec{s} \times \vec{r}}{r^3}$$

$$\frac{d\vec{r}}{dt} = \frac{dx}{dt} \vec{i}_x + \frac{dy}{dt} \vec{i}_y = \frac{dr}{dt} \vec{i}_r + r \frac{d\theta}{dt} \vec{i}_\theta$$

$$\oint \vec{E} \cdot d\vec{r} = -\frac{d}{dt} \int \vec{B} \cdot d\vec{S}$$

$$C = \frac{Q}{V} = \frac{A\epsilon_0}{d} \quad R = \rho \frac{l}{A}$$

$$\int \vec{B} \cdot d\vec{S} = \pm Li$$

$$\oint \vec{B} \cdot d\vec{r} = \mu_0 i_{enclosed}$$

$$\frac{d \ln U}{dx} = \frac{dU}{dx} \frac{1}{U}$$

1.

2.

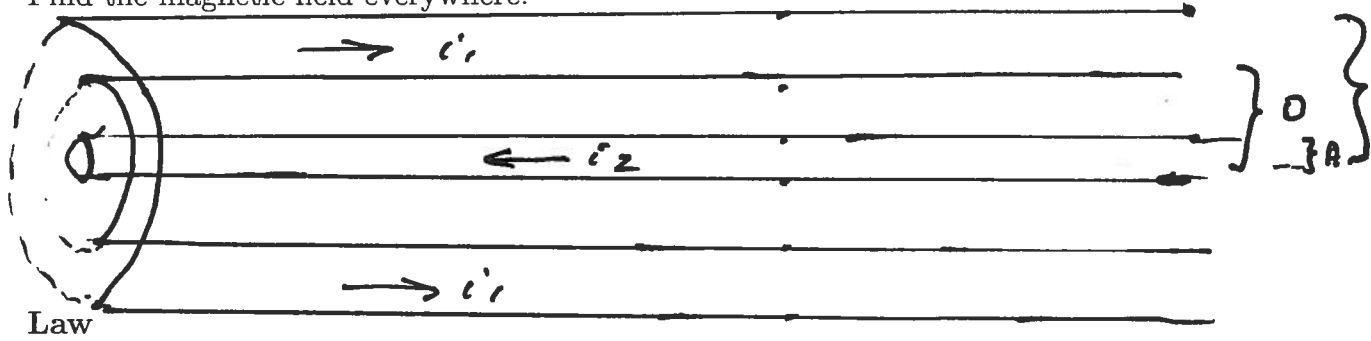
3.

4.

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Please mark all charges and currents on the appropriate figure so that your symbols are defined. Do not waste time on non-trivial integrals.

1. (25 points) Consider an infinitely long, hollow cylindrical wire. The wire has outer radius  $F$  and the cylindrical hole at its center has radius  $D$ . A current  $i_1$  flows from left to right and the current is uniformly spread over the region between  $F$  and  $D$ . At the center of this wire is an infinitely long cylindrical wire of radius  $A$ . It has a current  $i_2$  flowing from right to left and that current is uniformly spread over its area. Find the magnetic field everywhere.

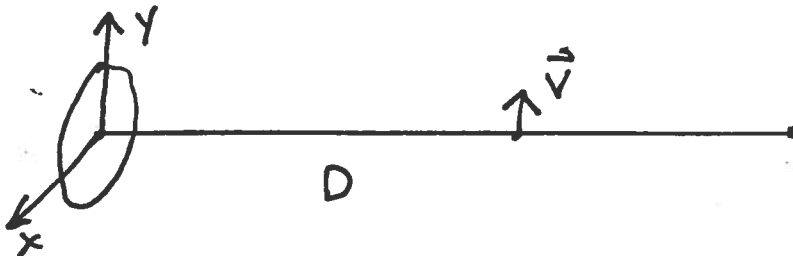


Law

Application

Result

2. (25 points) A very thin circle of wire lies in the  $x, y$  plane. It has radius  $R$ . A positively charged particle, charge  $q$ , is a distance  $D$  away from the center of the circle moving with a velocity  $\vec{v}$  as shown. The force on the particle when it is at the point shown is measured and has the known magnitude  $F$  and points into the page, in the negative  $x$  direction. What is the current in the circle of wire?

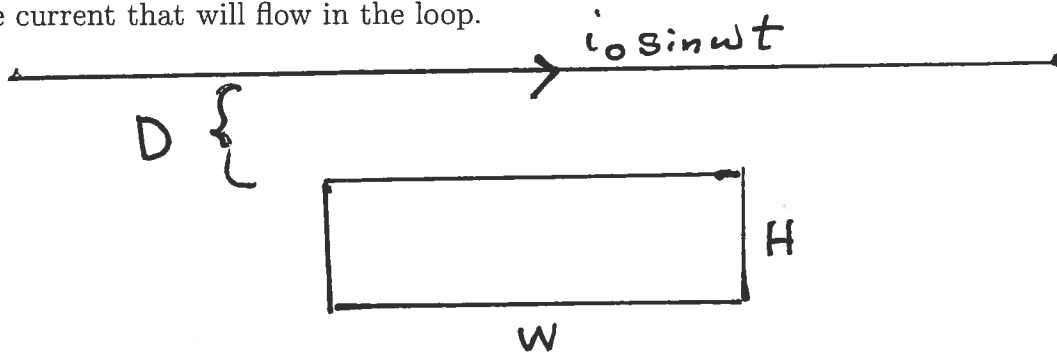


Law

Application

Result

3. (25 points) An infinitely long wire carries a current  $i_0 \sin \omega t$  as shown, where  $i_0$  and  $\omega$  are known. Nearby is a rectangular loop of wire with resistivity  $\rho$  which has cross sectional area  $A$  and dimensions  $W$  and  $H$  as shown. Ignoring self inductance find the current that will flow in the loop.



Law

Application

Result

4. (25 points) A circular loop of wire has resistance  $R$  and contains a capacitor with capacitance  $C$ . It is in the horizontal plane. There is a constant vertical magnetic field of magnitude  $B_0$  pointing up. At time  $t = 0$  the loop begins to mysteriously expand so that its area is given by  $A(t) = A_0(1 + \gamma t)$  where  $\gamma$  and  $A_0$  are known constants. (The resistance does not change during this expansion.) Find the charge on the capacitor as a function of time. (Ignoring self inductance.)



**Law**

**Application**

**Result**