

EXAM I Physics 218

Name.....Section Number.....

(1 point)

USEFUL INFORMATION

$$\text{If } f(x) = kx^n \quad \frac{df}{dx} = nkx^{n-1}$$

$$\text{If } f(x) = kx^n \quad \int f(x)dx = \frac{1}{n+1}kx^{n+1} + C$$

Make sure it is clear how you arrive at your solutions

1.

2.

3.

1. (33 points) This is a one dimensional problem. An object is dropped from a height H above the ground. Defining vertically up to be the positive direction the object experiences an acceleration

$$a(t) = \beta t - g$$

where β is a known constant.

- a. Obtain an algebraic equation for the velocity as a function of time.

- b. Obtain an algebraic equation for the height as a function of time.

- c. Find the time, T , at which the object reaches its lowest point, assuming this occurs before it hits the ground.

2. (33 points) A small block of mass m is placed on the frictionless floor which we define to be the x, y plane. There are two forces, \vec{F}_1 and \vec{F}_2 , acting on the block that have components only in the x, y plane. Because of these forces the block moves in a very strange way so that its position vector is observed to be

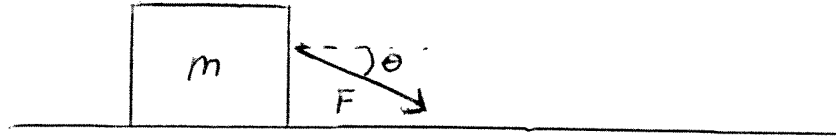
$$\vec{r}(t) = (c_1t^3 + c_2t)\vec{i} + (c_3t^2 + c_4t)\vec{j}.$$

Here all the c 's are known constants. One of the forces is known to be given by

$$\vec{F}_1 = k_1\vec{i} + k_2t\vec{j}.$$

Here k_1 and k_2 are known constants. What is the other force?

3. (33 points) A block of mass m is at rest on a table. A force of known magnitude $|\vec{F}| = F$ acts on the block, at the known angle θ as shown:



- a. Assuming no friction between the table and the block, isolate the block and show all forces acting on it. (In other words draw the free body diagram for the block.)
- b. Find the acceleration of the block.
- c. Now assume there is a coefficient of friction μ between the table and the block. Find the acceleration of the block assuming the force \vec{F} is large enough to make the block move.
- d. Find the minimum value that $|\vec{F}|$ must have in order to cause the block to move.