

Answers 1st Exam 2012

1. a) $x(t) = \frac{c_1 t^2}{2} + \frac{c_2 t^3}{3} + D$

b) $a(t) = c_1 + 2c_2 t$

c) $\vec{A} + \vec{B} + \vec{C} = (-B \sin \theta_1 + C \cos \theta_2) \vec{i} + (-A + B \cos \theta_1 + C \sin \theta_2) \vec{j}$

2. a) $x_a(t) = v_B \cos \theta t$

$y_a(t) = -\frac{1}{2} g t^2 + v_B \sin \theta t + S$

b) $v_B \cos \theta t^* = D$

$-\frac{1}{2} g t^{*2} + v_B \sin \theta t^* + S = H$

or $-\frac{1}{2} g \frac{D^2}{v_B^2 \cos^2 \theta} + v_B \sin \theta \frac{D}{v_B \cos \theta} + S = H$

3. a) $-g T_{\text{top}} + \frac{c_1 T_{\text{top}}^2}{2} + v_R = 0$

b) $-\frac{g T_{\text{grad}}^2}{2} + \frac{c_1 T_{\text{grad}}^3}{6} + v_R T_{\text{grad}} + H = 0$

4. a) $x_{\text{car}}(t) = \frac{1}{2} a_x \cos \theta t^2 + v_x \cos \theta t$
 $y_{\text{car}}(t) = \frac{1}{2} a_y \sin \theta t^2 + v_y \sin \theta t$

b) $x^r(t) = -\frac{c_2 t^4}{12} - v_w \cos \beta t + D$
 $y^r(t) = \frac{c_1 t^3}{6} + v_w \sin \beta t + S$

c) $\left. \begin{aligned} x_{\text{car}}(t^*) &= x^r(t^*) = \frac{H}{\tan \theta} \\ y_{\text{car}}(t^*) &= y^r(t^*) = H \end{aligned} \right\}$